

EECS 360  
Spring 2021  
Analog Filtering

1. Let  $H(f) = \text{tri}(f/1000)$ 
  - a) Find the first zero bandwidth.
  - b) Find the 3dB bandwidth.
  - c) Find the equivalent rectangular bandwidth
  
2.
  - a)  $x(t) = 10000 \text{sinc}^2(10000t)$ ,  $x(t)$  is input to an ideal lowpass filter with a bandwidth of  $B$  kHz find the smallest  $B$  such that the filter introduces no distortion.
  - b) Find the % energy in the frequency range  $|f| \leq 5000$  ?
  - c) What are the barriers to building the filter described in part a)
  
3. Let  $x(t) = \sum_{k=-\infty}^{\infty} \text{rect}\left(\frac{t - T_o k}{w}\right)$  where  $w = 1 \mu\text{s}$  and  $T_o = 2 \mu\text{s}$ 

Design (specify) a system (filter) to convert  $x(t)$  to  $y(t) = \cos(2\pi f_a t)$  where  $f_a = 1.5 \text{ MHz}$ .
  
4. A series R, L, C circuit is modeled by the following differential equation with  $x(t)$ =input voltage and  $y(t)$ =output voltage=voltage across the capacitor.
$$LC \frac{d^2 y(t)}{dt^2} + RC \frac{dy(t)}{dt} + y(t) = x(t)$$
  - a) Find  $H(f)$ .
  - b) Plot  $20 \log_{10}(|H(f)|)$  with  $R=100 \text{ Ohm}$ ,  $L=0.001 \text{ Henry}$ ,  $C=0.000001 \text{ Farad}$ . (You are encouraged to use Matlab to do this plot.)
  - c) For  $R=100 \text{ Ohm}$ ,  $L=0.001 \text{ Henry}$ ,  $C=0.000001 \text{ Farad}$ , given  $x(t) = \cos(2\pi 1760t)$  find  $A$  in  $y(t) = A \cos(2\pi 1760t + \phi)$
  - d) Is 1760 Hz close to the 3 dB bandwidth for this system?

Confirm your results with:

[http://www.ittc.ku.edu/~frost/EECS\\_360/Mathematica-360/Series-RLC-Transfer-Functions.cdf](http://www.ittc.ku.edu/~frost/EECS_360/Mathematica-360/Series-RLC-Transfer-Functions.cdf)